

# TRACE EXPANSIONS AND EQUIVARIANT TRACES FOR AN ALGEBRA OF SHUBIN TYPE FOURIER INTEGRAL OPERATORS ON $\mathbb{R}^n$

**Speaker: Elmar Schrohe**  
**Leibniz Universität Hannover**

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## Abstract:

We consider the algebra  $\mathcal{B}$  of all operators on  $\mathcal{S}(\mathbb{R}^n)$  given as finite sums

$$B = \sum R_g T_w A,$$

where

- $A$  is a pseudodifferential operator in the Shubin calculus on  $\mathbb{R}^n$
- For  $w = a - ik \in \mathbb{C}^n$ ,  $T_w$  is the Heisenberg-Weyl operator given by  $T_w u(x) = e^{ikx - iak/2} u(x - a)$ ,  $u \in L^2(\mathbb{R}^n)$
- $g \mapsto R_g$  represents  $g \in U(n) \subset Sp(2n)$  as a metaplectic operator, using the identification  $\mathbb{C}^n \cong T^*\mathbb{R}^n$ .

It is a consequence of Egorov's theorem for metaplectic operators that this is indeed an algebra.

Choosing an auxiliary operator such as  $H = |x|^2 - \Delta$ , we obtain expansions for

- $\text{Tr}(B(H - \lambda)^{-K})$  in powers of  $\lambda$  and  $\log \lambda$  for  $K$  large, as  $\lambda \rightarrow \infty$  in a sector of  $\mathbb{C}$ ,
- $\text{Tr}(B e^{-tH})$  as  $t \rightarrow 0^+$  in powers of  $t$  and  $\log t$ , and
- the pole structure of the meromorphic extension of  $\zeta_B(z) = \text{Tr}(B H^{-z})$ .

Moreover, we find a noncommutative residue that extends the Wodzicki residue to this situation. For a discrete subgroup  $G$  of  $\mathbb{C} \rtimes U(n)$  this allows us to define equivariant traces on  $\mathcal{B}$ .

Joint work with Anton Savin, RUDN University, Moscow, Russia.