

**ON TOPOLOGICAL TILINGS AND SHIFT EMBEDDABILITY
FOR ACTIONS OF AMENABLE GROUPS**

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Zoom meeting: 502 398 6833 Password: 721994

Abstract:

Let $G \curvearrowright X$ be a free action of an amenable group on a compact metrizable space. The shift embeddability problem asks whether there exists a G -equivariant embedding of X into the M -cubical shift $([0, 1]^M)^G$, and over the years it has become one of the central questions in the mean dimension theory. The best-known result to date was the theorem of Gutman, Qiao, and Tsukamoto, which provides a satisfying answer for actions of \mathbb{Z}^d . In this talk, we will describe how this theorem can be generalized to actions of amenable groups from a larger class. After stating the main results, we will focus on the parts of the proof that required a different approach from that of GQT, specifically:

- 1) defining the right notion of a tiling,
- 2) encoding the tilings using a small amount of information, and
- 3) obtaining the tiling from an a priori weaker property.