

***DYNAMIC BEHAVIOUS OF THE ITERATION OF THE TRACE  
MAPPING ASSOCIATED WITH SUBSTITUTIVE SEQUENCE***

**Speaker: Professor Zhiying Wen**

**Tsinghua University**

**Time: Tuesday, April 1, 2025, 15:00-16:00**

**Venue: Room 1801, East Main Guanghai Tower**

**Abstract:** 介绍一类由代换律生成的无穷序列引入的3D动力系统，该系统涉及到数学的一些不同的分支，报告将介绍系统的一些基本性质，和其它学科的联系和一些问题。

## DIMENSION OF DIVERGENCE POINTS RELATED TO $L^u$ ROTH EXPANSION

**Speaker:** Professor Wenxia Li  
East China Normal University

**Time:** Tuesday, April 1, 2025, 16:00-17:00

**Venue:** Room 1801, East Main Guanghua Tower

**Abstract:** Associated to the  $L^u$  roth expansion of an irrational number  $\bar{x} \in (0, 1)$  is a sequence  $x = \{x_i\} \in \mathbb{N}^{\mathbb{N}}$ . Then for each  $n$ , one can get an infinite probability vector  $\Pi(x|n) = (p_{i,n})_{i \in \mathbb{N}}$  where  $p_{i,n}$  is the frequency of  $i$  occurring in the prefix of  $\{x_i\}$  of length  $n$ . Let  $A(\{\Pi(x|n)\}_{n \in \mathbb{N}})$  be the set of accumulation points of the sequence  $\{\Pi(x|n)\}_{n \in \mathbb{N}}$ . Given a set  $C$ , let

$$\Omega_{\{=C\}} = \left\{ x \in \mathbb{N}^{\mathbb{N}} : A(\{\Pi(x|n)\}_{n \in \mathbb{N}}) = C \right\};$$

$$\Omega_{\{\subseteq C\}} = \left\{ x \in \mathbb{N}^{\mathbb{N}} : A(\{\Pi(x|n)\}_{n \in \mathbb{N}}) \subseteq C \right\}.$$

In this talk, we mainly present the Hausdorff dimensions of  $\Omega_{\{=C\}}$  and  $\Omega_{\{\subseteq C\}}$ . This is a joint work with Y. X. Gui and Y. Zhou.