Week 2 (Sep.18-Sep.22)

Topic: Incompressible Navier-Stokes Equations

Workshop Room: Room 2201, Guanghua East Building, Fudan University

Lecture Series Speakers: Hideo Kozono (Waseda University)

Invited Speakers: Guilong Gui (Northwest University) Bin Han (Hangzhou Dianzi University) Ning Jiang (Wuhan University) Qi Zhang (University of California Riverside) Zhifei Zhang(Peking University)

Organizing Committee:

Peter Constantin (Princeton University) Yoshikazu Giga (University of Tokyo) Hao Jia (University of Chicago) Carlos Kenig (University of Chicago) Zhen Lei (Fudan University) Fanghua Lin (Courant Institute of Mathematical Sciences) Gregory Seregin (University of Oxford) Vladimir Sverak (University of Minnesota) Edriss Titi (Texas A & M University) Sijue Wu (University of Michigan)

Sponsored by

Shanghai Center for Mathematical Sciences School of Mathematical Sciences, Fudan University

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Schedule

2017 Fall Program on Analysis of PDE (Sept. 11 – Dec. 2, 2017)

Week 2 (Sept.18-Sept.22)		
Topic: Incompressible Navier-Stokes Equations		
Monday (September 18) Room 2201, Guanghua East Building, Fudan University		
Morning Session		
9:30 – 9:35	Chair: Fanghua Lin	
9:35 – 10:25	Hideo Kozono (Lecture 1)	
10:25 - 10:45	Tea Break	
10:45 - 10:50	Chair: Hideo Kozono	
10:50 - 11:40	Jiang Ning	
Lunch Break		
Afternoon Session		
14:30 - 14:35	Chair: -	
14:35 – 15:25	Free	
15:25 – 15:45	Tea Break	
15:45 – 15:50	Chair: -	
15:50 - 16:40	Free	
Tuesday (September 19) Room 2201, Guanghua East Building, Fudan University		
Morning Session		
9:30 – 9:35	Chair: Fanghua Lin	
9:35 – 10:25	Hideo Kozono (Lecture 2)	
10:25 - 10:45	Tea Break	
10:45 - 10:50	Chair: Jiang Ning	
10:50 - 11:40	Zhang Qi	
Lunch Break		

Afternoon Session		
14:30 - 14:35	Chair: -	
14:35 – 15:25	Free	
15:25 – 15:45	Tea Break	
Group Photo	15:45 – 16:00	
16:00 - 16:05	Chair: -	
16:05 - 16:55	Free	
Wednesday (Septembe	er 20) Room 2201, Guanghua East Building, Fudan University	
Morning Session		
9:30 - 9:35	Chair: Fanghua Lin	
9:35 – 10:25	Hideo Kozono (Lecture 3)	
10:25 - 10:45	Tea Break	
10:45 - 10:50	Chair: Zhang Qi	
10:50 - 11:40	Zhang Zhifei	
Lunch Break		
Afternoon Session		
14:30 - 14:35	Chair: -	
14:35 – 15:25	Free	
15:25 – 15:45	Tea Break	
15:45 – 15:50	Chair: -	
15:50 - 16:40	Free	
Thursday (September 21) Room 2201, Guanghua East Building, Fudan University		
Morning Session		
9:30 - 9:35	Chair: Fanghua Lin	
9:35 – 10:25	Hideo Kozono (Lecture 4)	
10:25 - 10:45	Tea Break	
10:45 - 10:50	Chair: Zhang Zhifei	
10:50 - 11:40	Guilong Gui	
Lunch Break		

Afternoon Session		
14:30 - 14:35	Chair: Guilong Gui	
14:35 – 15:25	Shangkun Weng	
15:25 – 15:45	Tea Break	
15:45 - 15:50	Chair: -	
15:50 - 16:40	Free	
Friday (September 22) Room 2201, Guanghua East Building, Fudan University		
Morning Session		
9:30 – 9:35	Chair: Fanghua Lin	
9:35 – 10:25	Hideo Kozono (Lecture 5)	
10:25 - 10:45	Tea Break	
10:45 - 10:50	Chair: Lei Zhen	
10:50 - 11:40	Han Bin	
Lunch Break		
Afternoon Session		
14:30 - 14:35	Chair: -	
14:35 – 15:25	Free	
15:25 – 15:45	Tea Break	
15:45 – 15:50	Chair: -	
15:50 - 16:40	Free	

2017 Fall Program on Analysis of PDE

Week 2 (Sep.18-Sep.22)

Topic: Incompressible Navier-Stokes Equations

Titles and Abstracts:

Speaker: Guilong Gui TBA

Speaker: Bin Han

Title: Sharp one component regularity for Navier-Stokes

Abstract: We consider the conditional regularity of mild solution $v\$ to the incompressible Navier-Stokes equations in three dimensions. Let $e \in in \mathbb{S}^2$ and $0 < T^{ast} < \inf v$. J. Chemin and P. Zhang (Ann. Sci. $'{E}c$. Norm. Sup $'{e}r$, 2016) proved the regularity of $v\$ on $(0,T^{ast})$ if there exists $p \in (4, 6)$ such that $\$ int_ $0^{T^{ast}} |v \ cdot e |^p_{dot} | ^{frac} 1 | 2 + frac 2 | p | dt < \inf v$. J. Chemin, P. Zhang and Z. F. Zhang (Arch. Ration. Mech. Ana. ,2017) extended the range of $p\$ to $(4, \sin ty)$. In this article we settle the case $p \in [2, 4]$. Our proof also works for the case $p \in (4, \sin ty)$.

Speaker: Ning Jiang

Speaker: Hideo Kozono

Title: Method of the Besov space and its applications to the strong solutions of the Navier-Stokes equations

Abstract: We first introduce several basic notions of the Besov spaces such as paraproduct formula and the chain rule. The bilinear estimates related to the nonlinear structure on the Navier-Stokes equations and the \$L^p-L^q\$-type estimates of the Stokes semigroup are established. Then the problem on existence, uniqueness and regularity of the stationary Navier-Stokes equations is discussed in the scaling invariant homogeneous Besov space. In particular, a self-similar solution is constructed. As for the non-stationary case, we prove a maximal regularity theorem of the Stokes equations in the homogeneous Besov space. Finally,

local and global well-posedness in the critical Besov space is fully investigated for the Cauchy problem with the external forces of the non-stationary Navier-Stokes equations.

This series of lectures is based on the joint work with Prof. Senjo Shimizu at Kyoto University.

Speaker: Shangkun Weng Title: On the decay properties of steady axisymmetric Navier-Stokes Abstract: TBA

Speaker: Qi Zhang Title: Regularity of Weak Solutions of Elliptic and Parabolic Equations with Some Critical or Supercritical Potentials

Abstract: We prove Holder continuity or differentiability of weak solutions of uniformly elliptic and parabolic equations with power like potentials which scales critically or super-critically. This is a joint work with Li Zijin.

Speaker: Zhifei Zhang TBA

Participants:

Dongfen Bian (Beijing Institute of Technology) Guilong Gui (Northwest University) Bin Han (Hangzhou Dianzi University) Bobo Hua (Fudan University) Ning Jiang (Wuhan University) Hideo Kozono (Waseda University) Zhen Lei (Fudan University) Hui Li (Peking University) Jingyue Li (China Academy of Engineering Physics) Fanghua Lin (Courant Institute) Xiang Luo (University of Science and Technology of China) Yao Nie (Beihang University) Peng Qu (Fudan University) Jiawei Sun (Capital Normal University) Houzhi Tang (Capital Normal University) Shangkun Weng (Wuhan University) Hao Wu (Fudan University) Qi Zhang (University of California, Riverside) Zhifei Zhang (Peking University) Qidi Zhang (Chinese Academy of Sciences) Yi Zhou (Fudan University)