

INDEPENDENT SETS IN MIDDLE TWO LAYERS OF BOOLEAN LATTICE

Online Seminar Speaker: Lina Li University of Illinois at Urbana-Champaign

Time: Thur, June. 25th, 10:00-11:00 Zoom meeting ID: 967 863 80622 Link: https://zoom.com.cn/j/96786380622

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Abstract: In recent decades, independent sets in the discrete hypercube has received a lot of attention from many notable researchers. The classical result of Korshunov and Sapozhenko in 1983 counts the number of independent sets in the hypercube, and then shows that typical independent sets are not far from the trivial construction. For an odd integer n=2d-1, let $\operatorname{CM}(n, d)$ be the subgraph of the hypercube induced by the two largest layers. Our new results describe the typical structure of independent sets in $\operatorname{CM}(n, d)$ and also give precise asymptotics on the number of them. The proofs use Sapozhenko's graph container lemma, and a recently developed method of Jenssen and Perkins, which combines Sapozhenko' s graph container lemma with a classcal tool from statistical physics, the cluster expansion for polymer models. This is a joint work with Jozsef Balogh and Ramon I. Garcia.